## Towers (4)

Place the numbers 1, 2, 3 and 4 in the bottom of a tower. Add the adjacent numbers to make the number above. What is the total at the top? $\qquad$


1. If you change the order of the numbers, do you get the same total at the top? Use the attached pyramid sheet to investigate.
$\qquad$
2. What is the highest and lowest possible total at the top?
$\qquad$
3. Try the numbers $2,3,4$ and 5 . What happens to the lowest and highest totals? Use the attached pyramid sheet to investigate.
$\qquad$
$\qquad$
$\qquad$
4. What would the highest and lowest totals be for $3,4,5$ and 6 ? Use the attached pyramid sheet to investigate.
$\qquad$
$\qquad$
$\qquad$
5. By writing the sums in each box, write the sum for the total at the top.


## Towers (4)

## Challenge (Formulas)

6. Replace the numbers in the bottom row with letters $a, b, c$ and $d$. Find the formula for the sum at the top.

7. What would the formula be for different-sized towers?

## Towers (4)



## Towers (5)

Place the numbers 1, 2, 3, 4 and 5 in the bottom of a tower. Add the adjacent numbers to make the number above. What is the total at the top? $\qquad$


1. If you change the order of the numbers, do you get the same total at the top? Use the attached pyramid sheet to investigate.
$\qquad$
2. What is the highest and lowest possible total at the top?
$\qquad$
3. Try the numbers $2,3,4,5$ and 6 . What happens to the lowest and highest totals? Use the attached pyramid sheet to investigate.
$\qquad$
$\qquad$
$\qquad$
4. What would the highest and lowest totals be for $3,4,5,6$ and 7 ? Use the attached pyramid sheet to investigate.
$\qquad$
$\qquad$
$\qquad$
5. By writing the sums in each box, write the sum for the total at the top.


## Towers (5)

## Challenge (Formulas)

6. Replace the numbers in the bottom row with letters $a, b, c, d$ and $e$. Find the formula for the sum at the top.

7. What would the formula be for different-sized towers?

## Towers (5)



## Answers

| Towers 4 | Towers 5 |
| :--- | :--- |
| Total 20 | Total 48 |
| 1. No | 1. No |
| 2. Highest 24, lowest 16 | 2. Highest 65, lowest 35 |
| 3. Highest 32, lowest 24 | 3. Highest 81, lowest 51 |
| 4. Highest 40, lowest 32 | 4. Highest 97, lowest 67 |
| 5. $1+2+2+2+3+3+3+4$ | $5.1+2+2+2+2+3+3+3+3+3+$ <br> $3+4+4+4+4+1$ |
| 6. $a+3 b+3 c+d$ | 6. $a+4 b+6 c+4 d+e$ |

7. The pattern uses Pascal's triangle.

| Tower | Pascal's Triangle |  |
| :--- | :---: | :---: |
| 1 | 1 | $a$ |
| 2 | 11 | $a+b$ |
| 3 | 121 | $a+2 b+c$ |
| 4 | 1331 | $a+3 b+3 c+d$ |
| 5 | 14641 | $a+4 b+6 c+4 d+e$ |
| 6 | 15101051 | $a+5 b+10 c+10 d+5 e+f$ |

In Pascal's triangle 1's go on the outside and add the adjacent numbers to find the number below.

